

# Processus à sauts, applications en finance et simulation (32h)

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## PROGRAM

After recalling basic facts concerning Brownian motion and the Black-Scholes formula, we turn to processes having jumps and introduce the concept of Lévy processes. A first part of the course is devoted to the investigation of basic properties of Lévy-processes (Lévy-Khintchine formula, the Lévy-Itô decomposition). Then we turn to questions that are at the heart of mathematical finance: the Girsanov theorem and the Itô formula for Lévy processes. We show how to apply these concepts for option pricing. The course is supplied by exercises.

### Detailed program

1. Processes in continuous time and Brownian motion.
2. General definition of Lévy processes, examples: Poisson process, compound Poisson process.
3. Poisson random measures (PRM) and integrals with respect to PRM
4. Lévy-Itô decomposition
5. Properties of sample paths of Lévy processes: finite/infinite activity, bounded/unbounded variation. Subordinators.
6. Lévy measures and moments
7. Margingales and Lévy measures
8. Girsanov's theorem and Esscher transform
9. Itô formula for Lévy processes
10. Option pricing: Lévy driven Market models, incompleteness, Fourier transform method for option pricing.
11. Simulation of Lévy processes

## References

- [1] Sato, K. (1999) “Lévy processes and infinitely divisible distributions”, Cambridge University Press.
- [2] Papapantoleon, A. (2008) “An introduction to Lévy processes with applications in finance”. <http://arxiv.org/abs/0804.0482>.
- [3] Cont, R., Tankov, P. (2004) “Financial Modelling with Jump Processes”. Chapman & Hall.
- [4] Carr, P., Geman, H., Madan, D.B., Yor, M.(2002) “The fine structure of Asset returns: An empirical investigation”. *Journal of Business* vol 75.
- [5] Voltchkova, E.(2005) “Integro-differential evolution equations: numerical methods and applications in finance”, PhD thesis, <http://tel.archives-ouvertes.fr/tel-00010842>.