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## 1.1 Réponse

$$I_1 R_1 = V_i - V \quad (1.1.1)$$

$$I_1 + I_c = I_2 \Rightarrow I_1 = I_2 - I_c$$

$$I_1 = \frac{V}{R_2} - (V_o - V) \times j\omega C$$

$$I_1 = V \times \left( \frac{1}{R_2} + j\omega C \right) - V_o \times j\omega C$$

$$V_o = A \times V_i$$

$$I_1 = V \times \left( \frac{1}{R_2} + j\omega C \right) - A \times V_i \times j\omega C$$

$$V = \frac{I_1 + A \times V_i \times j\omega C}{\frac{1}{R_2} + j\omega C} \quad (1.1.2)$$

Il faut mettre l'équation 1.1.2 dans la l'équation 1.1.1.

$$I_1 R_1 = V_i - \left( \frac{I_1}{\frac{1}{R_2} + j\omega C} + \frac{A \times V_i \times j\omega C}{\frac{1}{R_2} + j\omega C} \right)$$

$$I_1 R_1 + \frac{I_1 R_2}{1 + j\omega R_2 C} = V_i - \frac{A \times V_i \times j\omega R_2 C}{1 + j\omega R_2 C}$$

$$I_1 \times (R_1 + R_2 + j\omega R_1 R_2 C) = V_i \times (1 + j\omega R_2 C - A \times j\omega R_2 C)$$

$$I_1 \times (R_1 + R_2 + j\omega R_1 R_2 C) = V_i \times (1 + j(1 - A) \times \omega R_2 C)$$

$$Z_i = \frac{V_i}{I_1} = \frac{(R_1 + R_2 + j\omega R_1 R_2 C)}{(1 + j(1 - A) \times \omega R_2 C)}$$

$$Z_i = \frac{(R_1 + R_2 + j\omega R_1 R_2 C)(1 - j(1 - A) \times \omega R_2 C)}{1 + (1 - A)^2 \omega^2 R_2^2 C^2}$$

$$Z_i = \frac{(R_1 + R_2 + (1 - A)\omega^2 R_1 R_2^2 C^2) + j\omega R_1 R_2 C - j(1 - A)\omega R_2 C (R_1 + R_2)}{1 + (1 - A)^2 \omega^2 R_2^2 C^2}$$

$$A > 1 \rightarrow \Re[Z_i] = \frac{R_1 + R_2 + (1 - A)\omega^2 R_1 R_2^2 C^2}{1 + (1 - A)^2 \omega^2 R_2^2 C^2} = 0$$

$$R_1 + R_2 = (A - 1)\omega^2 R_1 R_2^2 C^2$$

$$\omega = \frac{1}{R_2 C} \sqrt{\frac{R_1 + R_2}{(A - 1)R_1}}$$